

Problem 2.10

Car A travels at 55 mi/hr. Car B travels at 70 mi/hr.

a.) Assuming they start at the same time, what's the difference in arrival times for a destination 10 miles away?

b.) How far must B travel to be 15 minutes ahead of A?

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a.) Assuming they start at the same time, what's the difference in arrival times for a destination 10 miles away?

$$x_2 = x_1 + v_1 t + \frac{1}{2} a t^2$$

$$\Rightarrow \Delta x_A = v_{1,A} t \quad (\text{as } a=0)$$

$$\Rightarrow (10 \text{ mi}) = (55 \text{ mi/hr}) t_A$$

$$\Rightarrow t_A = .182 \text{ hrs}$$

and

$$x_2 = x_1 + v_1 t + \frac{1}{2} a t^2$$

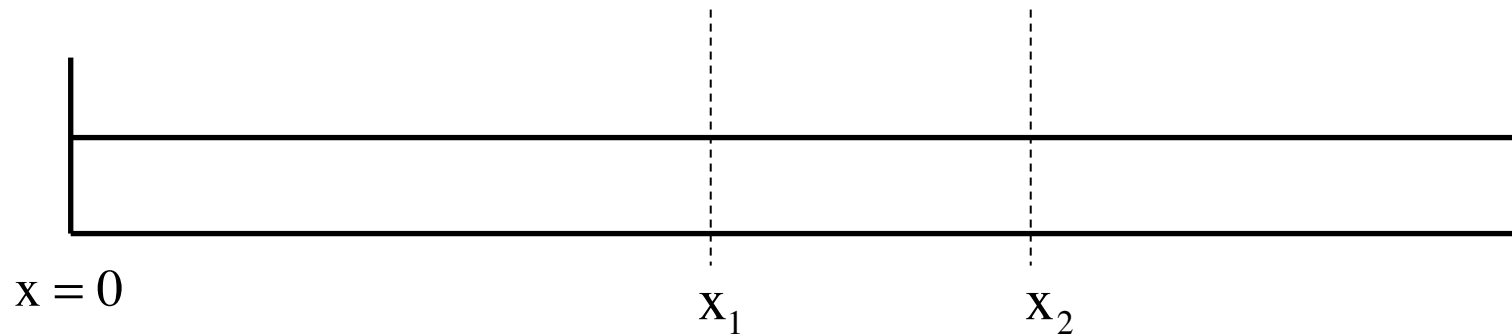
$$\Rightarrow \Delta x_B = v_{1,B} t_B \quad (\text{as } a=0)$$

$$\Rightarrow (10 \text{ mi}) = (70 \text{ mi/hr}) t_B$$

$$\Rightarrow t_B = .143 \text{ hrs}$$

$$\text{so } \Delta t = .182 - .143 = .039$$

b.) How far must B travel to be 15 minutes ahead of A?



Assume car B is at x_2 at time t and car A is at x_1 at that same point in time. The difference between those two points must equal to the distance car A travels in a quarter of an hour. With that, we can write:

$$\begin{aligned}x_1 &= v_A t & \text{and} & & x_2 &= v_B t \\ &= (55 \text{ mi/hr})t & & & &= (70 \text{ mi/hr})t \\ &= 55t & & & &= 70t\end{aligned}$$

From car A

$$\begin{aligned}\Delta x &= x_2 - x_1 = 70t - 55t = 15t \\ &= v_A (.25) \\ &= (55)(.25) \\ \Rightarrow t &= .92 \text{ sec} \Rightarrow x_2 = v_B t = (70 \text{ mph})(.92 \text{ sec}) \\ &= 64.4 \text{ mi}\end{aligned}$$